





# The Multi Level Multi Domain method (MLMD) for Particle In Cell plasma simulations

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# Outline

- PI: motivations: beyond the Implicit Moment Method
- P2: the Multi-Level Multi-Domain (MLMD) method
- P3: collisionless magnetic reconnection: the essential facts
- P4: MLMD simulations of collisionless magnetic reconnection
- P5: MLMD simulations of turbulence
- P6: conclusions

#### PI: Sample of the physical problems tackled with the Implicit Moment Method (IMM) code iPic3D



Magnetic field switch-off in PIC simulations of collisionless magnetic reconnection with guide field M.E. Innocenti et al.



Solar wind - Lunar Magnetic Anomaly interaction J. Deca et al.



Markidis et al., 2010

#### PI: Sample of the physical problems tackled with the Implicit Moment Method (IMM) code iPic3D

What do these simulations have in common?

#### computational cost $\sim 10^5$ -10<sup>6</sup> core hours, a significant fraction of a standard PRACE Tier 0 allocation



## PRACE: pan-European supercomputing infrastructure

| RANK | SITE  | SYSTEM  | CORES     | (TFLOP/S) | (TFLOP/S) | (KW)   |
|------|---|---|-----------|-----------|-----------|--------|
| 1    | National Super Computer Center in<br>Guangzhou<br>China               | Tianhe-2 (MilkyWay-2) - TH-IVB-FEP<br>Cluster, Intel Xeon E5-2692 12C 2.200GHz,<br>TH Express-2, Intel Xeon Phi 31S1P<br>NUDT | 3,120,000 | 33,862.7  | 54,902.4  | 17,808 |
| 2    | DOE/SC/Oak Ridge National Laboratory<br>United States                 | Titan - Cray XK7, Opteron 6274 16C<br>2.200GHz, Cray Gemini interconnect, NVIDIA<br>K2Dx<br>Cray Inc.                         | 560,640   | 17,590.0  | 27,112.5  | 8,209  |
| 3    | DOE/NNSA/LLNL<br>United States  | Sequoia - BlueGene/Q, Power BQC 16C 1.60<br>GHz, Custom<br>IBM  | 1,572,864 | 17,173.2  | 20,132.7  | 7,890  |
| 4    | RIKEN Advanced Institute for<br>Computational Science (AICS)<br>Japan | K computer, SPARC64 VIIIfx 2.0GHz, Tofu<br>interconnect<br>Fujitsu  | 705,024   | 10,510.0  | 11,280.4  | 12,660 |
| 5    | DOE/SC/Argonne National Laboratory<br>United States                   | Mira - BlueGene/Q, Power BQC 16C<br>1.60GHz, Custom<br>IBM  | 786,432   | 8,586.6   | 10,066.3  | 3,945  |
| 6    | Swiss National Supercomputing Centre<br>[CSCS]<br>Switzerland         | Piz Daint - Cray XC30, Xeon E5-2670 8C<br>2.600GHz, Aries interconnect , NVIDIA K20x<br>Cray Inc.                             | 115,984   | 6,271.0   | 7,788.9   | 2,325  |
| 7    | King Abdullah University of Science and<br>Technology<br>Saudi Arabia | Shaheen II - Cray XC40, Xeon E5-2698v3 16C<br>2.3GHz, Aries interconnect<br>Cray Inc.   | 196,608   | 5,537.0   | 7,235.2   | 2,834  |
| 8    | Texas Advanced Computing Center/Univ. of<br>Texas<br>United States    | Stampede - PowerEdge C8220, Xeon E5-<br>2680 8C 2.700GHz, Infiniband FDR, Intel<br>Xeon Phi SE10P<br>Dell                     | 462,462   | 5,168.1   | 8,520.1   | 4,510  |
| 9    | Forschungszentrum Juelich (FZJ)<br>Germany                            | JUQUEEN - BlueGene/Q, Power BQC 16C<br>1.600GHz, Custom Interconnect<br>IBM   | 458,752   | 5,008.9   | 5,872.0   | 2,301  |

#### top 500 list (June 2015)

RMAX

RPEAK

POWER

## PI:Which are the "expensive" phases of an iPic3D simulation?







Np >> Ng "particle dominated" regimes Np: particle # Ng: grid points #



judge - 4x2x2

judge - 4x4x4

Percentage Execution Time

Scalasca profiling with different input parameters: most of the simulation time is spent in particle- related operations

judge - 4x4x2

juqueen - 16x16x8

Why is the number of particles high?

- numerical noise proportional to I/ √Np → minimum number of particles per cell to be kept
- large domains to be simulated with high spatial resolutions  $\rightarrow$  high Ng  $\rightarrow$  high Np
- Np is proportional to (m<sub>i</sub>/m<sub>e</sub>)<sup>D/2</sup>, with m<sub>i</sub>/m<sub>e</sub> mass ratio and D problem dimensionality (with fixed ion scale domain size, fixed electron scale resolution and increasing mass ratio between particle species)

## PI:Which are the "expensive" phases of an iPic3D simulation?



particle species)

### PI:Adaptive techniques for Particle In Cell (PIC) simulations

Moving Mesh Adaptation (MMA)

Brackbill, 1993, Delzanno 2008, Lapenta, 2011, Chacon 2011

fixed number of grid points; points are attracted in the "interesting" part of the domain, according to a monitor quantity Adaptive Mesh Refinement (AMR)

Vay, 2004, Fujimoto et Sydora, 2008

changing number of grid points; cells are split or coalesced, according to a monitor quantity; all existing AMR codes are explicit





#### Multi-Level Multi-Domain (MLMD)

Innocenti, 2013; Beck, 2014; Innocenti, 2015

different grid levels are simulated with different spatial and temporal resolution; the IMM method is used →the advantages of the IMM and of adaptivity are harnessed together

#### P2: The Multi-Level Multi-Domain (MLMD) method: a semi-implicit adaptive method for Particle In Cell plasma simulations



- the different levels are simulated fully with fields and particles with different spatial and temporal resolutions
   → the highest resolution is used only when needed
- → ion and (when resolved) electron processes are correctly resolved, at a much lower computational cost
  - realistic mass ratios are cheaply handled: ion scale resolution on one level, electron scale resolution on the other
  - the IMM grants more freedom in the choice of the local resolutions, in the limits of the stability constraint  $0.1 < v_{th,e} dt/dx < 1$ (explicit algorithms have to resolve inverse electron plasma frequency, Debye length, smaller, for stability reasons)

#### The MLMD terminology:

jump in *spatial* resolution: Refinement Factor RF jump in *temporal* resolution: Time Ratio TR lower resolution grid: Coarse Grid (CG) higher resolution grid: Refined Grif (RG)

#### P2: The stability constraint of the IMM and the MLMD system

Implicit Moment Method (IMM) stability constraint



"large" dx  $\rightarrow$  Finite Grid Instability (FGI) sampling is not frequent enough; spurious high frequencies give non-physical electric field oscillations and particle heating



 $\rho^{n+\theta} = \sum_{p} q_{p} S(\mathbf{x} - \mathbf{x}^{n+\theta}) = \sum_{p} q_{p} \left[ S(\mathbf{x} - \mathbf{x}^{n}) + (\mathbf{x}^{n+\theta} - \mathbf{x}^{n}) \nabla S(\mathbf{x} - \mathbf{x}^{n}) + \frac{1}{2} (\mathbf{x}^{n+\theta} - \mathbf{x}^{n})^{2} \nabla \nabla S(\mathbf{x} - \mathbf{x}^{n}) + \mathcal{O}(\mathbf{x} - \mathbf{x}^{n})^{3} \right]$ 

 $(\mathbf{x}^{n+\theta} - \mathbf{x}^n) = f(\mathbf{E}^{n+\theta})$ 

 $S(\mathbf{x} - \mathbf{x}^n)$ 

assumption for Taylor expansion used in the IMM broken  $\rightarrow$ inaccurate results



dx/di=0.078

with fixed time step across the MLMD system,

the Coarse Grid risks falling into this regime

Harris field in magnetic reconnection with FGI

FGI can be suppressed with field smoothing!

FGI suppressed with field smoothing

dx/di=0.078

 $S(\mathbf{x}-\mathbf{x}^{n+ heta})$  particle shape function at "future" time

particle shape function at current time

with fixed time step across the MLMD system, the Refined Grid risks falling into this regime

different time steps have to be used at the different levels  $\rightarrow$  temporal sub-stepping

#### P2: A MLMD coarse grid iteration with sub-stepping



#### P2: Grid interlocking operations

I. Boundary condition interpolation (C2R)

 $\Xi_{I,g_{l+1}} = \sum_{g_l} \Xi_{N,g_l} W_{g_l} (\mathbf{x}_{g_l} - \mathbf{x}_{g_{l+1}})$ 

2. Refined field projection (R2C)

$$\mathbf{E}_{P,g_{l}} = \frac{1}{2} \left( \mathbf{E}_{N,g_{l}} + \mathbb{P}^{g_{l+1} \to g_{l}} \left( \mathbf{E}_{N,g_{l}+1} \right) \right)$$
$$\mathbb{P}^{g_{l+1} \to g_{l}} \left( \mathbf{E}_{N,g_{l}+1} \right) = \frac{\sum_{g_{l+1}} \mathbf{E}_{N,g_{l+1}} W_{g_{l}}(\mathbf{x}_{g_{l}} - \mathbf{x}_{g_{l+1}})}{\sum_{g_{l+1}} W_{g_{l}}(\mathbf{x}_{g_{l}} - \mathbf{x}_{g_{l+1}})}$$



**Coarse Level Particle** 

3. Boundary refined particle repopulation (C2R)

Particles sitting at the boundaries of the Refined Grid are generated according to the velocities and positions of corresponding Coarse Grid particles for consistent particle motion between CG and RG at the grid boundaries



 $q_{p_{g_{l+1}}}^{\rm t0+dt} = q_{p_{g_l}}^{\rm t0+dt} / RF^2$ 

the aim is to preserve the combined particle shape function and the distribution function at the boundaries elect

electron hole merging phase in a ID3V MLMD two stream instability with RF=4



#### P2: Grid interlocking operations

I. Boundary condition interpolation (C2R)

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**Refined Level Particles** 

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Particles sitting at the boundaries of the Refined Grid are generated according to the velocities and positions of corresponding Coarse Grid particles for consistent particle motion between CG and RG at the grid boundaries

-8

-9

-10

Superimposed,  $\omega_{pe}t=92$ 0.5 v×/c 0 -0.5 2 8 10 6 x/d

the aim is to preserve the combined particle shape function and the distribution function at the boundaries

electron hole merging phase in a ID3V MLMD two stream instability with RF=4



#### P2: Computing resource saving

Comparing the computing cost of MLMD simulations with single level simulations, resolved everywhere with the highest MLMD resolution



single level, highest resolution

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Comparing the computing cost of MLMD simulations with single level simulations, resolved everywhere with the highest MLMD resolution



#### P3: Collisionless magnetic reconnection: the essential facts

Magnetic reconnection is a change in the magnetic field line connectivity associated to fast energy release  $\rightarrow$  stored magnetic field energy is converted into kinetic energy and heat

Magnetic reconnection is a key process in astrophysical and space plasmas  $\rightarrow$  e.g. Sun-Earth connection and space weather

Sweet-Parker vs Petschek vs fast kinetic reconnection

under which conditions does reconnection happen?



#### P3: Collisionless magnetic reconnection: the essential facts



in collisionless magnetic reconnection (without guide field), fast reconnection is given by species separation - Hall term:

ions decouple first (heavier)

- electrons decouple last → species separation, Electron and Ion Diffusion Regions\*
  - in- plane currents lead to out of plane magnetic field Bz → characteristic quadrupolar structure\*
- in- plane electric field is given by Hall term in generalized Ohm's law\*



\* verify during Hands on

EHall Y

3.0000-04



 $\frac{1}{0 \text{ mega ci } t = 24.250}$ 

Birn 2001, 2007

#### P3: Energetically relevant regions in magnetic reconnection

The J.E metric [Goldman15] highlights the areas where the electric field does work on particles in magnetic reconnection  $\rightarrow$  areas relevant under the energetic point of view<sup>\*</sup>

\* verify during Hands on



∆<sub>IDR</sub>~ d<sub>i</sub> (ion skin depth) ; ∆<sub>EDR</sub>~ d<sub>e</sub> (electron skin depth)\*; d<sub>i</sub>/d<sub>e</sub>= √(m<sub>i</sub>/m<sub>e</sub>)
 Also, in IDR electrons are still magnetised → processes of interest at the ion scale in EDR, electrons are unmagnetised too → processes of interest at the electron scale
 → MLMD to retain the significant physical processes in the different regions, at a very low computational cost

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#### P4: MLMD simulations of magnetic reconnection

ion scale processes are resolved by both grids; electron scale processes (e.g., speed of electron jets\*) are simulated by both grids but fully resolved on the refined grid only; on the coarse grid, selective damping and spectral compression are at work



#### P4: MLMD simulations of magnetic reconnection

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Electron scale processes are reproduced by the refined grid e.g.: formation of jets at the X point with velocity  $v_{A,e}$ 



#### P4: MLMD simulations of magnetic reconnection

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Electron scale processes are reproduced by the refined grid e.g.: formation of jets at the X point with velocity  $v_{A,e}$ 



#### P5: MLMD simulations of turbulence generated by the Lower Hybrid Drift Instability (LHDI)

Other fields of application of the MLMD method: cases when multiple scales coexist self-similarly in a large domain

 $\rightarrow$  a representative part of the large domain is simulated with higher resolution

![](_page_22_Figure_3.jpeg)

the refined grid is driven by the coarse grid in the low wavenumber range; the refined grid cascades to the small scales which the coarse grid averages out Daughton 2003

#### P5: MLMD simulations of turbulence generated by the Lower Hybrid Drift Instability (LHDI)

Other fields of application of the MLMD method: cases when multiple scalea coexist self-similarly in a large domain

 $\rightarrow$  a representative part of the large domain is simulated with higher resolution

e.g.: simulations of Lower Hybrid Drift Instability.

The LHDI:

 I) is driven by a density gradient in presence of a perpendicular field
 2) is unstable over a large range of wavenumber and frequencies;
 fast branch with γ~Ω<sub>LH</sub>, k~I/ρ<sub>e</sub>, ES, slow branch at k~I/√(ρ<sub>e</sub>ρ<sub>i</sub>)~20, EM

 3) breaks large scale fields in smaller and smaller structures → acts as a "turbulence generator"

electron density

B<sub>z</sub> field component

![](_page_23_Picture_7.jpeg)

the refined grid is driven by the coarse grid in the low wavenumber range; the refined grid cascades to the small scales which the coarse grid averages out Daughton 2003

#### P5: simulations of turbulence: challenges and MLMD solutions

![](_page_24_Figure_1.jpeg)

In turbulent environment, energy is transported from the large to the small scales over several wavenumber decades (inertial range); the turbulent cascade is often broken by wave- particle interaction processes e.g.: candidate for the solar wind: interaction of protons with kinetic Alfven wave, proton cyclotron damping, electron or ion Landau

damping

large scales of energy injection

small scales of energy dissipation

high computational cost! Also, the number of particle has to be very high to reduce the numerical noise and grid effects (when using a PIC code) have to be taken into consideration

single level simulation

MLMD simulation

![](_page_24_Figure_9.jpeg)

![](_page_24_Figure_10.jpeg)

the particle noise plateau is pushed to higher k and lower power levels (more particles per unit volume)

the RG extends the k range of a factor RF with respect to the coarse grid; the computational cost is \*2 rather than \*RF<sup>2</sup>

#### P5: MLMD simulations of turbulence generated by the LHDI

Norgren 2012 observes coupling between the perpendicular electric field and magnetic field oscillations in the magnetotail in presence of LHDI waves at wavenumbers corresponding to the electrostatic LHDI branch with the perpendicular electron current as mediator. We confirm their observations and extend the study to lower wavenumber (electromagnetic LHDI branch, kink instability)

![](_page_25_Figure_2.jpeg)

Innocenti et al, in preparation

#### P5: Cluster observations confirming our findings

magnetotail, [-10 -3 3] RE GSM

the study done in Norgren 2012 for the fast ES LHDI branch is extended to the slow EM one

Bz, E perp coupling at both slow and fast LHDI branch as expected from our study

![](_page_26_Figure_4.jpeg)

## Conclusions

- The Multi-Level Multi-Domain method is a fully kinetic, semi-implicit adaptive method to reduce the cost of Particle In Cell Implicit Moment Method plasma simulations; we target in particular realistic mass ratio simulations
- the MLMD method has been demonstrated in two kinds of scenarios:

   problems where small scale, high frequency processes are confined in a small portion of the entire domain e.g.: magnetic reconnection
   self-similar processes where only a representative part of the domain is simulated with higher resolution e.g.: Lower Hybrid Drift Instability
- in both cases, the physical processes of interest are correctly reproduced, at a lower computational cost
  - during the Hands On: verify the multi scale nature of collisionless magnetic reconnection, as simulated with iPic3D